## LIST OF ENTRANCE EXAM QUESTIONS

FOR THE INTERNATIONAL MASTER'S DEGREE PROGRAM

# ітмо

### **BIG DATA AND MACHINE LEARNING**

#### **Differential Equations, Probability theory & Optimization Methods**

- 1. Ordinary differential equations (ODE). The Cauchy problem. ODEs of Higher order and ODEs systems.
- 2. Differential Equations in Partial Differential coefficient of the First Order. First integrals. General solution. The Cauchy problem.
- 3. Combinatorics: permutation, combinations.
- 4. Classical definition of probability, random events, sample space, power set, properties of classical probability.
- 5. Conditional probability. A theorem on total probability formula, Bayes' rule.
- 6. Random variable: definition, distribution function of a random value and its properties, independent random variables.
- 7. Definitions of numerical characteristics for discrete and continuous random variables: mean, dispersion, mode, median, moments.
- 8. Law of large numbers.
- 9. Central limit theorem.
- 10. Approximation and interpolation of functions.
- 11. Numerical integration.
- 12. Numerical methods for solving a system of linear algebraic equations.
- 13. Numerical methods for solving a system of nonlinear equations.
- 14. Optimization problems. Types of optimization problems.
- 15. Nonlinear programming problem. Methods of local and global optimization.
- 16. Methods for a local extremum search for the multidimensional optimization problem.
- 17. Methods for a global extremum search for the multidimensional optimization problem.
- 18. PCA, SVD. Definitions, relation.

#### Programming

- 19. Static data structures: vectors, arrays, tables.
- 20. Data structures: lists (stack / queue / deque, operations, application).
- 21. Hierarchical data structures: trees (types, storage, operations).
- 22. Data structures: heaps (types, construction, algorithms). Hashing.
- 23. Data structures: graphs (storage, basic algorithms on graphs).
- 24. Algorithm's complexity (concept, an estimation of complexity with the examples of sort and search algorithms)
- 25. Imperative and declarative programming. Most popular paradigms.
- 26. Object-oriented programming. Encapsulation. Inheritance. Polymorphism. SOLID.
- 27. Design patterns: creational, structural, and behavioral patterns.
- 28. Concurrency & Parallelism. Definition, differences, problems.
- 29. Database transactions: properties, main principles.
- 30. Indexes in databases. Aims, internal structures.

#### **RECOMMENDED READING**

- 1. Cormen, T. H., Leiserson, C. E., Rivest, R. L., & Stein, C. (2009). Introduction to algorithms. MIT press.
- 2. Bruce, P., Bruce, A., & Gedeck, P. (2020). Practical statistics for data scientists: 50+ essential concepts using R and Python. O'Reilly Media.
- 3. Strang, G., Strang, G., Strang, G., & Strang, G. (1993). Introduction to linear algebra (Vol. 3). Wellesley, MA: Wellesley-Cambridge Press.
- 4. Gautschi, W. (2011). Numerical analysis. Springer Science & Business Media.

## · · · · · · · · · · · · ·

